



A New Version of Grain-128 with Authentication

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1 Introduction

Motivation and Goals

2 The Old Grain-128

The Algorithm

Attacks and Observations

3 The New Grain-128a

The New Grain-128a

Authentication

4 Conclusion



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Authentication

4 Conclusion



Motivation and Goals

- ▶ Grain-128 is lightweight but some nonlinearities are too lightweight.
- ▶ Some applications need built-in authentication
- ▶ ...but leaving it out should be possible.
- ▶ Allow for easy updating of existing implementations.
- ▶ ...and trust!



Outline

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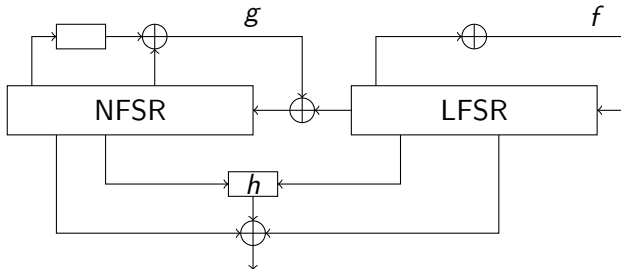
The New Grain-128a

Authentication

4 Conclusion



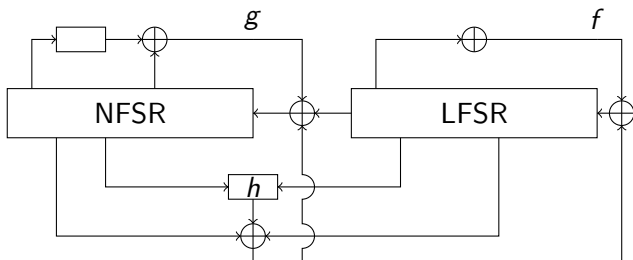
The Old Grain-128



- ▶ 128-bit key, 96-bit IV.
- ▶ An LFSR provides a large period.
- ▶ An NFSR with degree two updates the state nonlinearly.
- ▶ An output function of degree three produces nonlinear output.
- ▶ State bits are added linearly to ensure resiliency.
- ▶ Initialize in 256 rounds: feed output into the registers.
- ▶ Make faster by duplicating Boolean functions.



IV Padding Sliding Property



- ▶ The 96-bit IV goes into a 128-bit register and is padded with 111...111. With high probability, a shifted key and a shifted IV will produce the exact same keystream, only with a shift. [Küçük06], [DeCaKüPre08]
- ▶ Related-key Chosen-IV. [LeeJeongSungHong08]



Too Little Nonlinearity or Initialization

- ▶ Cube, 237/256 [AumDinHenMeiSha09]
- ▶ Maxterm, 256/256 [Stankovski10]

Looking at the first keystream bits, the equations, in unknown key bits, are not complicated enough.



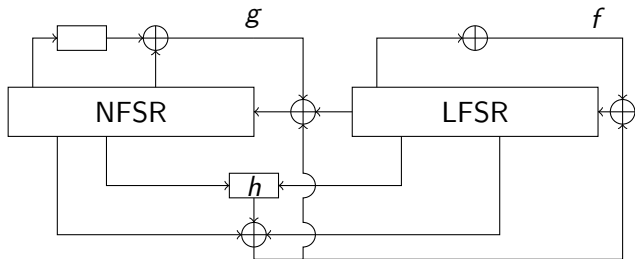
Too Little Nonlinearity and Similar Bits

- ▶ Chosen-IV (cube): Assuming ten specific key bits to be zero, the equations simplify “enough”. [DinSha11]



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- ▶ Also, b_{i+95} and s_{i+95} are multiplied together. During initialization, they are too similar, meaning the complexity doesn't grow as much as wanted.



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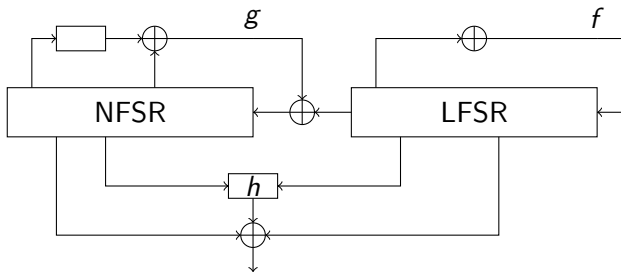
The New Grain-128a

Authentication

4 Conclusion



Changes from Grain-128



Grain-128 with changes:

- ▶ Pad the IV with $111\dots 110$.
- ▶ NFSR has nonlinearity **four**.
- ▶ Change a tap into the output function:
 b_{i+95} , s_{i+94} , so that we don't multiply bits that are “similar”.



Authentication

The above algorithm is used to produce *pre-output stream*.
Use different parts of it for different things:

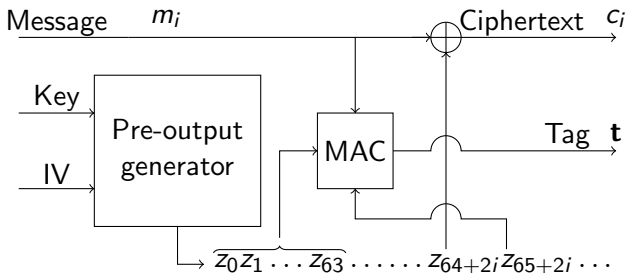
- ▶ Encryption
- ▶ Authentication



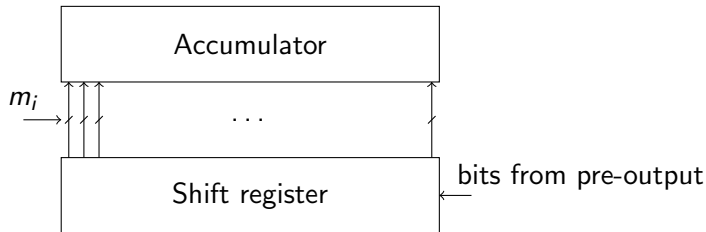
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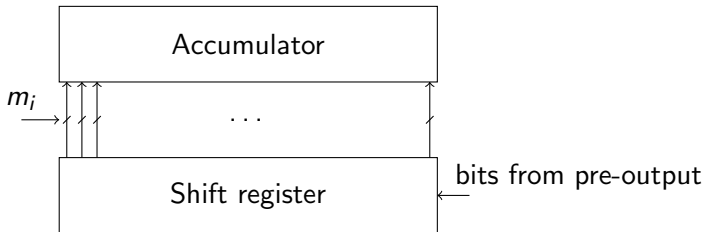
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- ▶ A Wegman-Carter approach.
- ▶ Initialize both registers with pre-output bits.
- ▶ We multiply the message bit vector by a Toeplitz matrix.



Authentication



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- ▶ Initialize both registers with pre-output bits.
- ▶ We multiply the message bit vector by a Toeplitz matrix.
- ▶ P_S is the prob. that an attack succeeds.
- ▶ With perfectly random input to the shift register, $P_S = 2^{-32}$.
- ▶ We have $P_S < 2^{-32} + 2\epsilon$. [Krawczyk95], [ÅHJ11], [Maximov06]



Hardware Characteristics

Several nice aspects:

- ▶ We can still increase the speed up to 32x.
- ▶ We can leave out the authentication.
- ▶ ...or part of it. w -bit tags for 2^{-w} .



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The cheapest one — a version that produces one bit per clock:

- ▶ Grain-128: 2133 gate equivalents
- ▶ Grain-128a: 2243 gate equivalents; a five per cent increase (as a bonus, we initialize faster.)

Adding authentication, we'd get a total of 2867 gate equivalents.



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Grain-128a

- ▶ is at least as secure than Grain-128,
- ▶ resists all current cryptanalysis on Grain-128,
- ▶ has optional authentication,
- ▶ is still hardware-efficient.



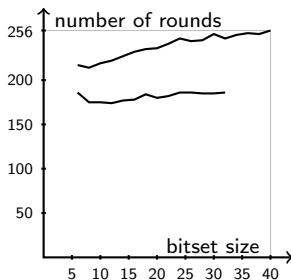
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Thank you!





On Cube/Maxterm/AIDA/...



How does a greedy strategy aid in finding good bitsets?

Upper curve: Stankovski's on Grain-128.

Lower curve: Ours on the pre-output of Grain-128a.

